Modeling Temporal Dynamics & Geographical Language Variations in Social Streams

Google

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- Motivation
- Modeling Social Streams
- Future work

- Motivation
- Modeling Social Streams
 - Modeling Popular Messages [WWW 2011]
 - Modeling Personal Decision & Content [WSDM 2013]
 - Empirical Topic Modeling Study [SOMA 2010]
 - Temporal Dynamics [KDD 2011]
 - Geographical Language Variations [WWW 2012]
- Future work

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- Modeling Social Streams
 - Modeling Popular Messages [WWW 2011]
 - Modeling Personal Decision & Content [WSDM 2013]
 - Empirical Topic Modeling Study [SOMA 2010]
 - Temporal Dynamics [KDD 2011]
 - Geographical Language Variations [WWW 2012]
- Future work

The Blossom of Social Media



Social Streams



acitrano @emilychang yes, there should. about 13 hours ago from

FriendFeed in reply to emilychang

Social Streams



Social Streams

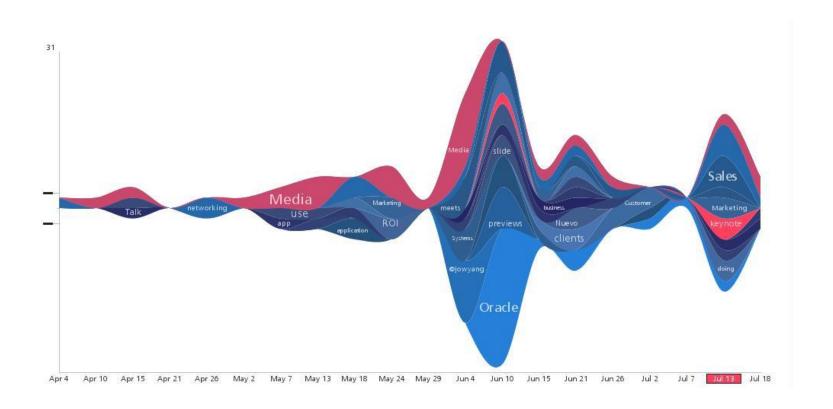


Social Streams



Challenges

Challenges: Temporal Dynamics



Challenges: Multiple Sources



Challenges: Meta-data



Challenges: Meta-data



Challenges

- Temporal dynamics
- Multiple sources
- Geographical locations

Technical Challenges

- Multi-facet data
- Large scale
- Incorporate other research advances

Temporal Dynamics + Multiple Sources Geographical Language Variations

Interesting Questions

Are here any common topics among multiple media sources?



Interesting Questions

- Are here any common topics among multiple media sources?
- How can we find them, automatically?



Interesting Questions

- Are here any common topics among multiple media sources?
- How can we find them, automatically?
- Are there transferred from one source to another?



Interesting Questions

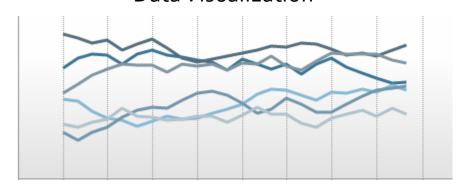
- Are here any common topics among multiple media sources?
- How can we find them, automatically?
- Are there transferred from one source to another?

[Zhao et al., ECIR 2011]



Applications

Data Visualization



Trend Prediction

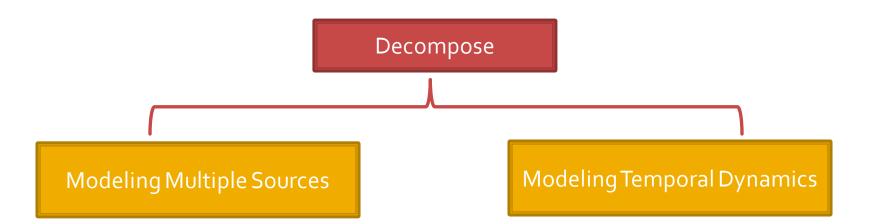


Goal

- identify common/local topics from multiple streams
- characterize their temporal dynamics
- *principled way*

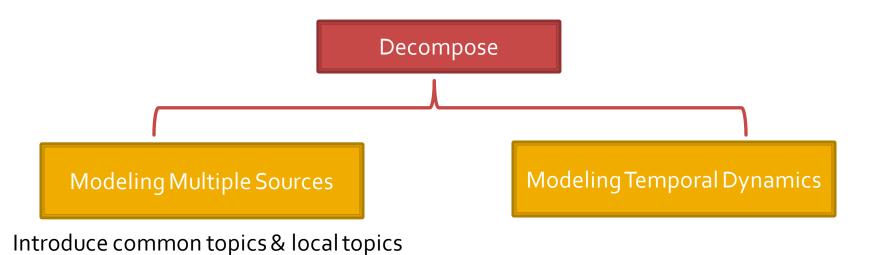
Modeling Temporal Dynamics Our Proposed Model

Our Approach



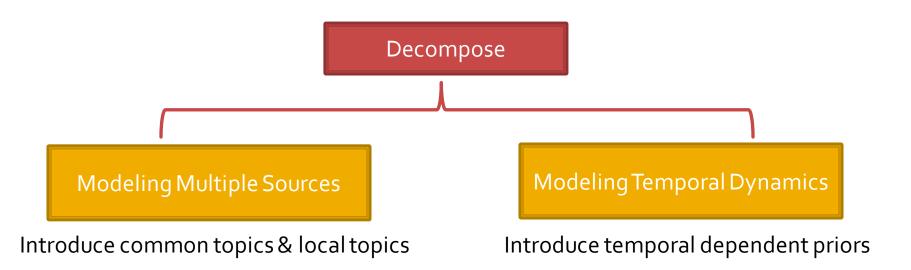
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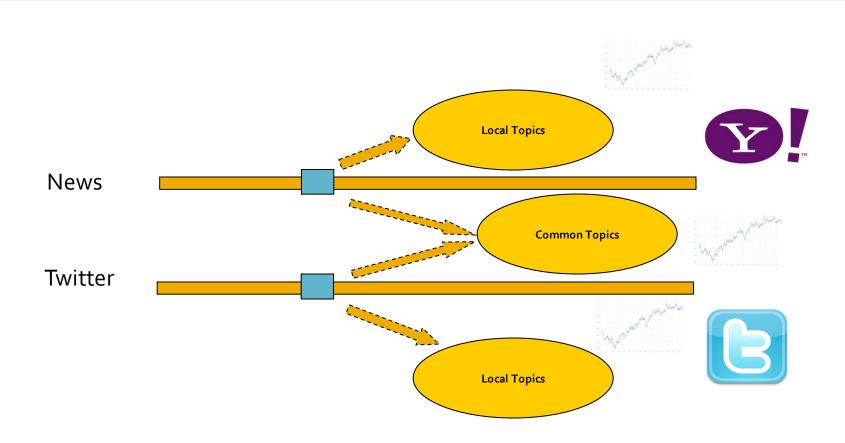


Modeling Temporal Dynamics Our Proposed Model

Our Approach



Modeling Temporal Dynamics Basic Setting



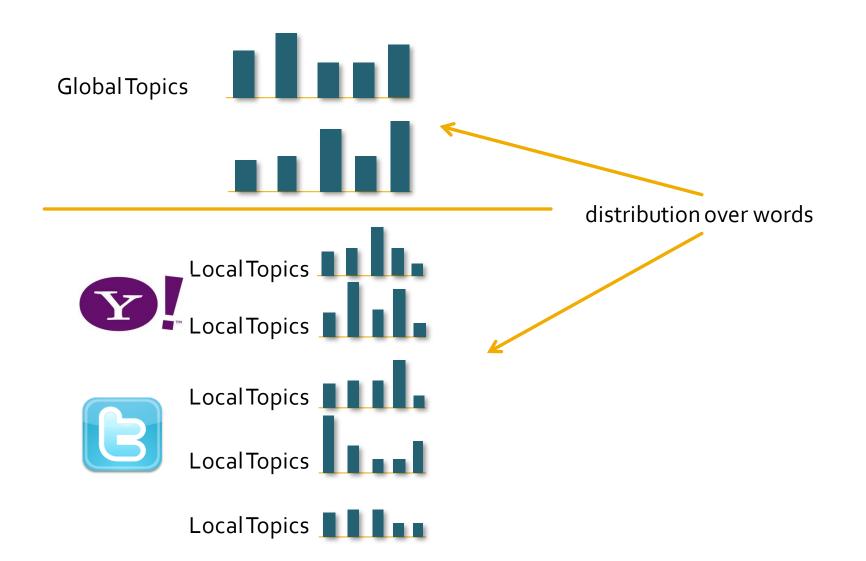
- Basic Intuitions
 - Some topics are shared.

Tsunami, Super bowl, NBA...

Some topics are specific to a certain stream.

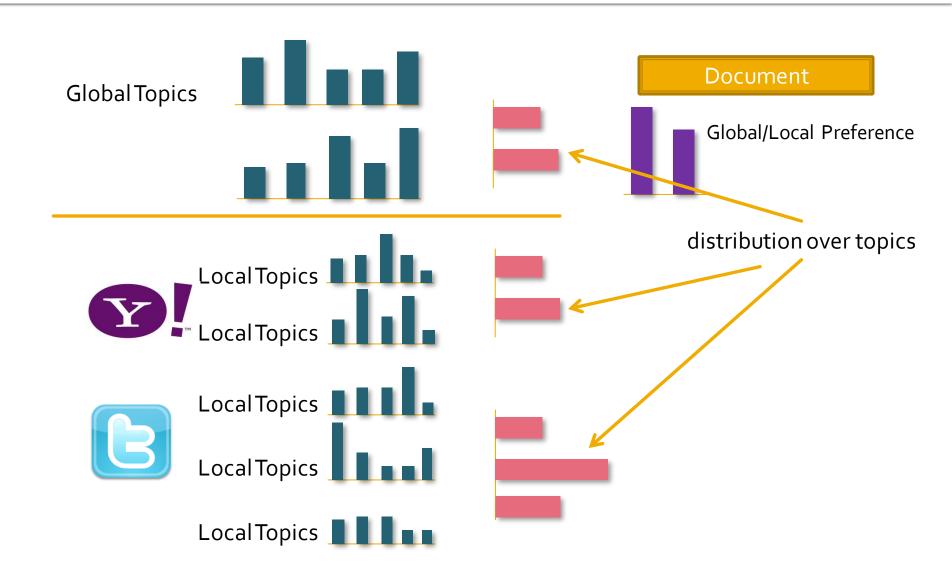
Local news, Personal opinions...

Each stream is a mixture of them.

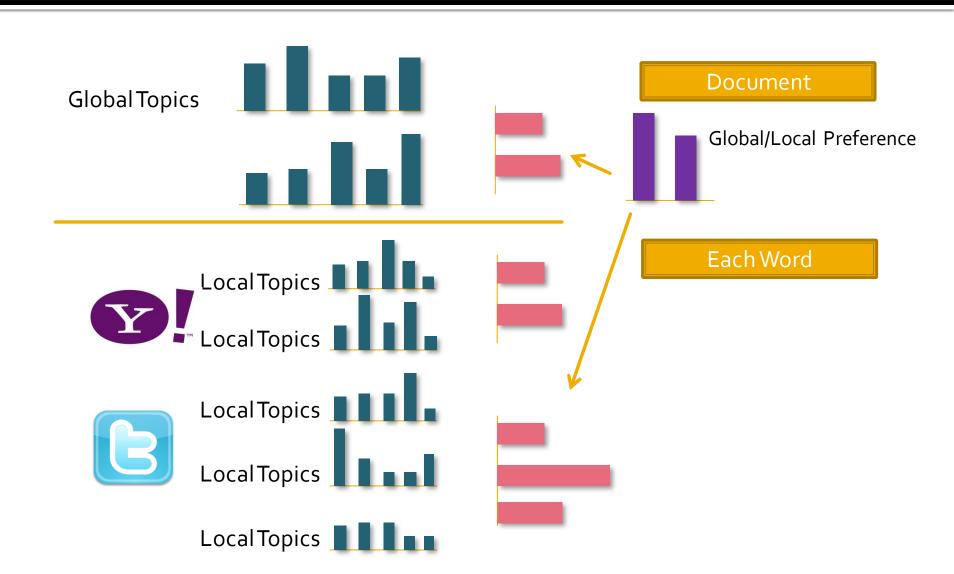




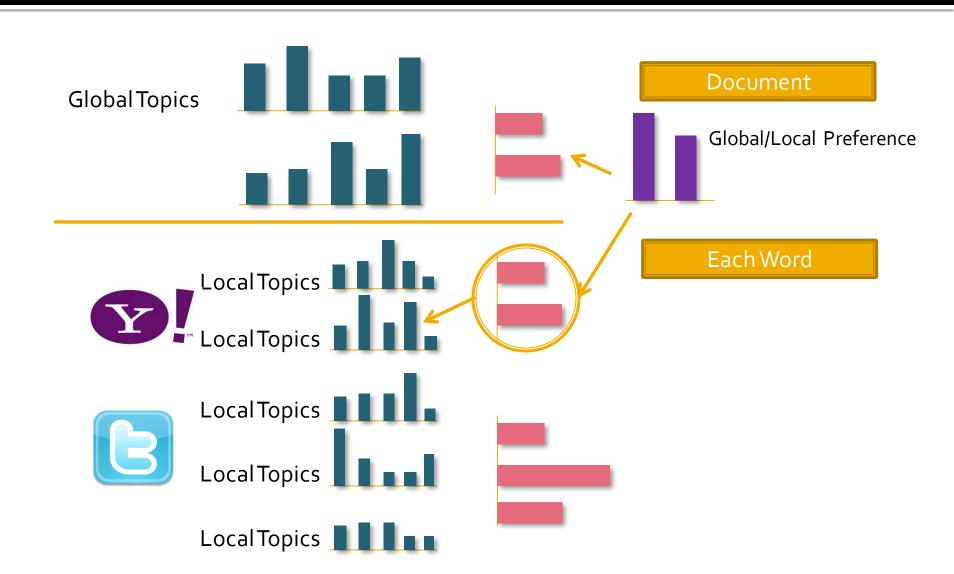






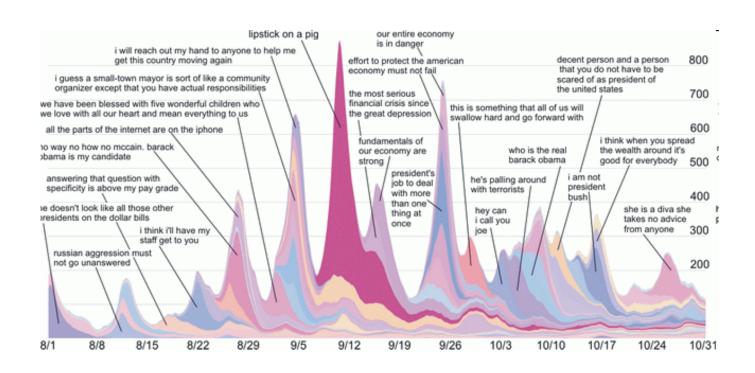






- Generative Process Summary:
 - Per-stream
 - Global/Local Preference Prior
 - Topic Prior
 - Language Model
 - Per-document
 - Global/Local Preference
 - Topic proportion
 - Per-token
 - Global/Local Choice
 - Topic Choice

Meme Tracking



Intuitions

Intuitions

Markovian Assumption

Intuitions

Markovian Assumption
 [Blei and Lafferty, ICML 2007]
 [Wang et al., UAI 2008]
 [Wei et al., IJCAI 2007]

Intuitions

- Markovian Assumption
- Use a function to characterize the changes of topic proportions over time

[Wang and McCallum, KDD 2006] [Yin et al., ICDM 2011]

Intuitions

- Markovian Assumption
- Use a function to characterize the changes of topic proportions over time
 - At certain time t, we will have higher prior probability to choose some

Assumptions

- Each topic only has one peak
- All topics are "trending"

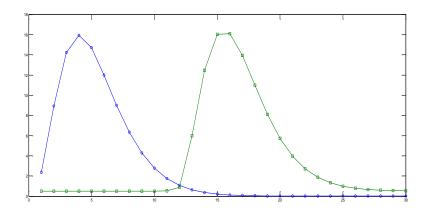
Assumptions

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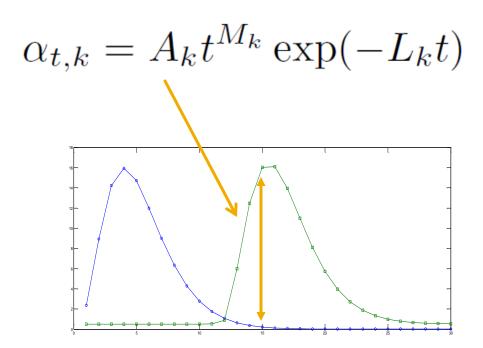
Yes, it's naïve & simplified & unrealistic...

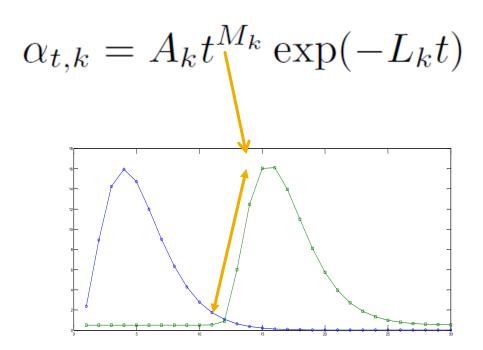
Temporal Function

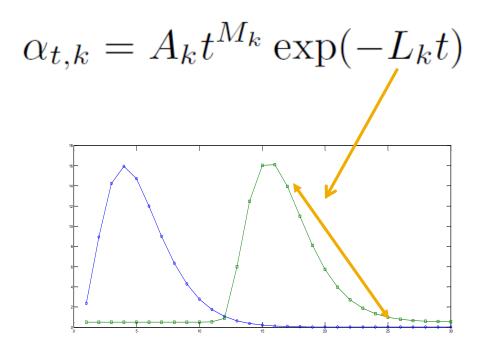
$$\alpha_{t,k} = A_k t^{M_k} \exp(-L_k t)$$



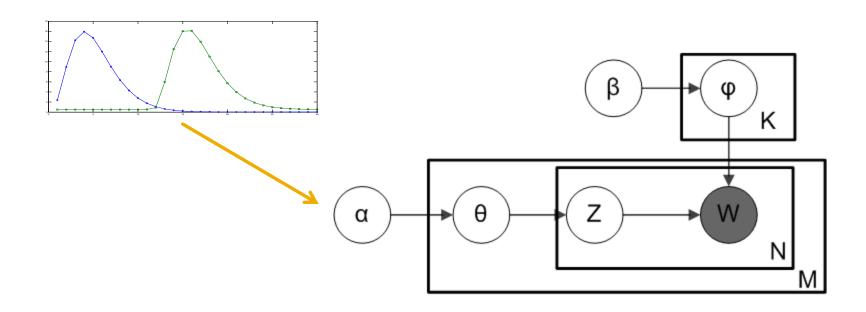
[Yang and Leskovec, WSDM 2011] [Leskovec et al., KDD 2009]







$$\alpha_{t,k} = A_k t^{M_k} \exp(-L_k t)$$



Temporal Modeling

- Overall Algorithm
 - EM-Style Algorithm
 - Gibbs Sampling in E-step
 - Functional Optimization in M-step Non-linear Least Square fit

Temporal Modeling

- Experiments & Conclusions
 - News & Tweets
 - 233,488 News articles
 - 1,736,350 Tweets
 - 720 hours in May, 2010

Temporal Modeling

Comparison of Top Ranked Common Topics between LDA (Left) and Temporal Collection (Right)					
Title	Top Terms	Title	Top Terms		
"finance"	percent billion bank market greece financial banks debt	"finance"	percent billion bank greece financial debt banks euro crisis		
"crime"	police car times vehicle found york square street bomb	"oil spill"	oil gulf spill coast drilling mexico water louisiana		
"junk"	link cont via #jobs #fb album super live wii #tcot #news	"world cup"	world cup team league final players south season club		
"oil spill"	oil gulf spill coast mexico gas drilling sea water	"health care"	health medical care cancer hospital patients study research		
"junk"	dont people cant thats youre bad look tell talk	"UK election"	minister party prime cameron political leader president		
Comparison of Local Topics between News (Left) and Twitter (Right)					
News		Twitter			
Title	Top Terms	Title	Top Terms		
"crime"	police car times vehicle found york square street	"social media"	blog video post check news via twitter online facebook		
"US election"	election party law president vote political campaign	"hash tags"	#fb info #quote #fail #ge #lol #ff #twibbon cont		
"China"	minister china south india north chinese korea indian	"non-English"	les pas pour sur une cest est qui avec bien suis tout faire		
"jobs"	budget tax million money pay bill federal increase cuts	"junk"	cant this wait watch next believe gonna watching just		
"education"	school students schools board education district college	"junk"	that would have could never were wish there		

Temporal Modeling

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Temporal Modeling

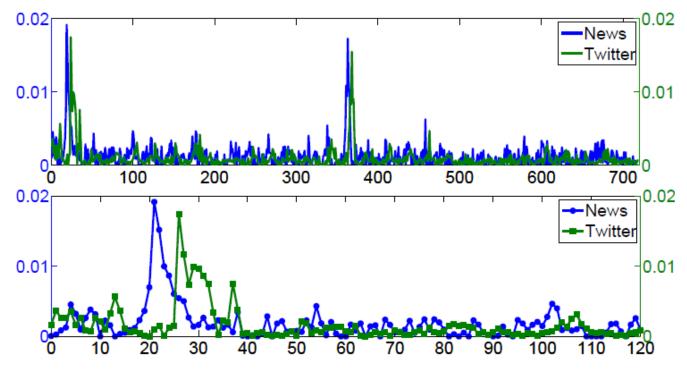
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Temporal Modeling

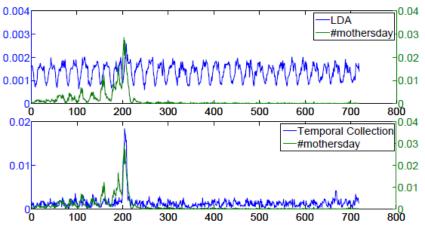
- Experiments & Conclusions
 Case Study on A Common Topic "Kentucky Derby"
 - Select a common topic which ranks the following terms high:
 - "derby", "race", "borel", "kentucky" and "horse" ...
 - Tracking temporal dynamics of a topic

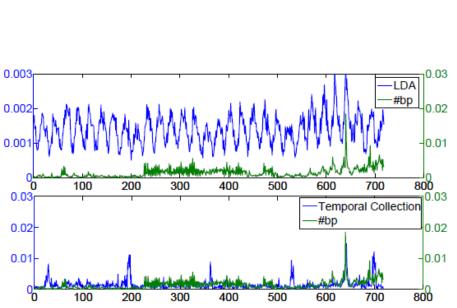


Temporal Modeling



Temporal Modeling





Temporal Dynamics & Geographical Language Variations

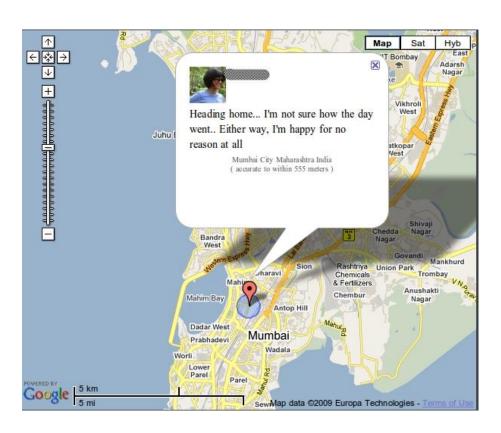
Conclusion

- A framework for modeling temporal dynamics for multiple sources.
- *Principled* way to tackle the problem.
- Bridge topic modeling & Information cascading.

Temporal Dynamics & Geographical Language Variations

Temporal Dynamics + Multiple Sources Geographical Language Variations

Social Stream + Locations





Interesting Questions

- How is information created and shared in different geographic locations? What is the inherent geographic variability of content?
- What are the spatial and linguistic characteristics of people? How does this vary across regions?
- Can we discover patterns in users' usage of microblogging services?

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- How is information created and shared in different geographic locations? What is the inherent geographic variability of content?
- What are the spatial and linguistic characteristics of people? How does this vary across regions?
- Can we discover patterns in users' usage of microblogging services?
- Can we predict user location from tweets?

Applications

Behavioral targeting and user modeling



Better local information filtering



Technical Challenges

- Tweets
 - noisy and short (140 characters)
- Only 1% of tweets geo-tagged
 - Can we predict locations for non-tagged tweets?
- Many intuitions to be combined
 - Background, regional language models, topics
 - Personal preferences, regional preferences...

. . .

Can we really infer locations for a tweet?

Yes via tweet decomposition

Just landed after a long flight. It is raining here at Lyon though!

What is the user's location?

Just landed after a long flight. It is raining here at Lyon though!

background

just after It be the can cant will

Just landed after a long flight. It is raining here at Lyon though!

Travel

landed flight delay TSE Gate terminal

background

just after It be the can cant will

Just landed after a long flight. It is raining here at Lyon though!

Travel/airport

landed flight delay TSE Gate terminal

background

just after It be the can cant will

SE airport area

Lyon
Saint
Exupery
convention
center
raining

Semantic Topic Background Language Model Regional Language Model

Travel/airport

landed flight delay TSE Gate terminal background

just after It be the can cant will SE airport area

Lyon
Saint
Exupery
convention
center
raining

Delayed again at the TSE check point and might miss my flight. way to go SF!

Travel/airport

landed flight delay TSE Gate terminal background

just after It be the can cant will **SFO**

SF SFO San Francisco airport

Can we always do that?

Life is good! Feeling great today!

Life is good! Feeling great today!

Daily life

life feeling good today morning background

just after It be the can cant will



Life is good! Feeling great today!

If we know something extra about the context and user location preferences, perhaps we can do better than random guessing!

Previous work

- Simple regional language models
 - No factorization
- No personal preferences
- Complicated inference algorithms
 - Usually two step process
 - Fails to learn coherent regions

- Motivations
- Our Proposed Model
- Experiments
- Conclusions

- A novel probabilistic model considers
 - Regional language models
 - Global topics
 - Personal preferences
- Sparse modeling + Bayesian treatment
- An efficient inference algorithm

- Basic Intuition
 - Regions
 - Topics
 - Users
 - Tweets
- The generative process
 - Intuition
 - Glory details

Modeling Geographical Language Variations Basic Intuition: Region

- Must be coherent
 - There is enough traffic in it
 - Affects the way we write tweets
 - Has preference over what topic discussed
 - Specific keywords
 - Area over the map
 - Example
 - An airport
 - A park
 - A mall
 - A city

Modeling Geographical Language Variations Basic Intuition: Topic

- Classify the content of the tweet
- Might not tell us the location
- Puts a distribution over words
- Examples
 - Sports
 - Politics
 - Travel
 - Daily life, etc

Modeling Geographical Language Variations Basic Intuition: User

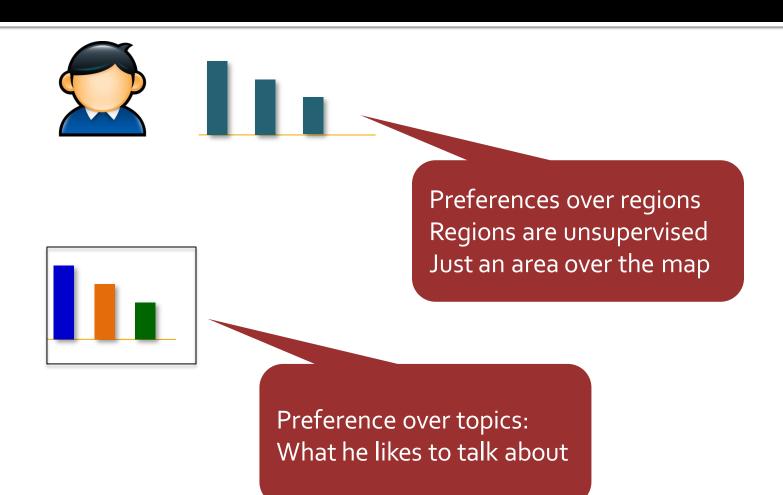
- Has preferences over locations
 - Where he usually spends his/her time
- Has preference over topics
 - What he tweets about

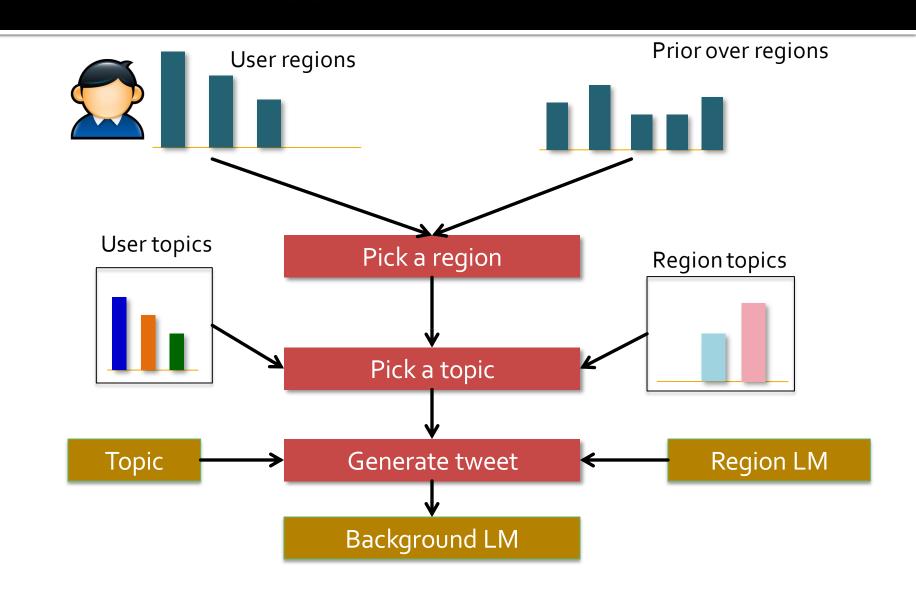
Modeling Geographical Language Variations Basic Intuition: Tweet

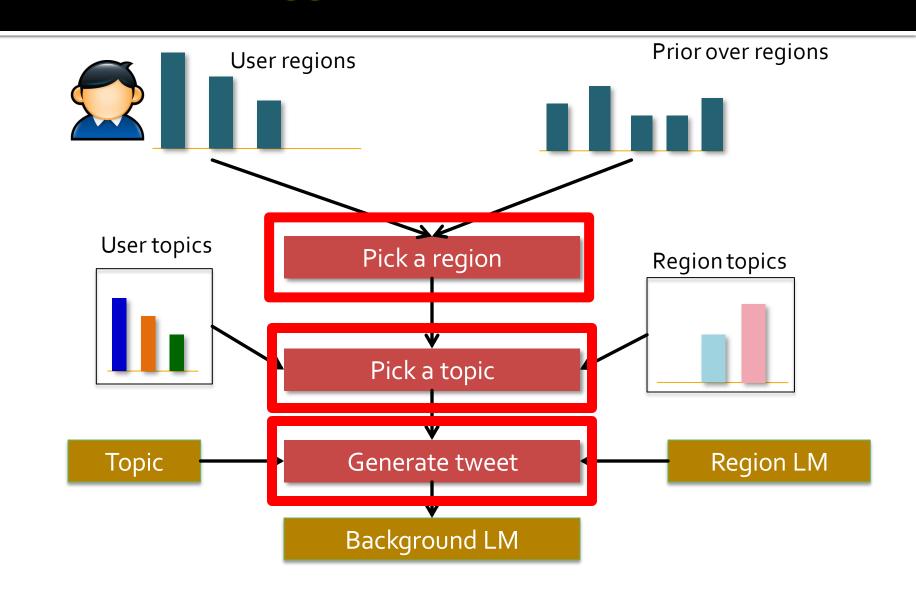
- Written by a given user
- At a specific location (region)
 - Depends on the user
- About a specific topic
 - Depends on
 - What the user talks about
 - What is being discussed at this location
- Composed of a bag of words from
 - Topic + location + background language models

- Basic Intuition
 - Regions
 - Topics
 - Users
 - Tweets
- The generative process
 - Intuitive explanation
 - Glory details

- Pick a location
- Pick a topic
- Generate the words







Modeling Geographical Language Variations Discrete Additive Models

- Switch-based models
 - Normalized distributions
 - Pick one distribution
 - Sample from it
- SAGE [Eisenstein et. al, 2011]
 - Un-normalized distribution
 - Log frequencies
 - Add them all together
 - Exponentiate and sample

An Additive model for discrete distributions

Discrete distribution via natural parameters
 Example:

$$p(v|\phi) = \exp(\phi_v - g(\phi))$$
 where $g(\phi) = \log \sum_v \exp(\phi_v)$

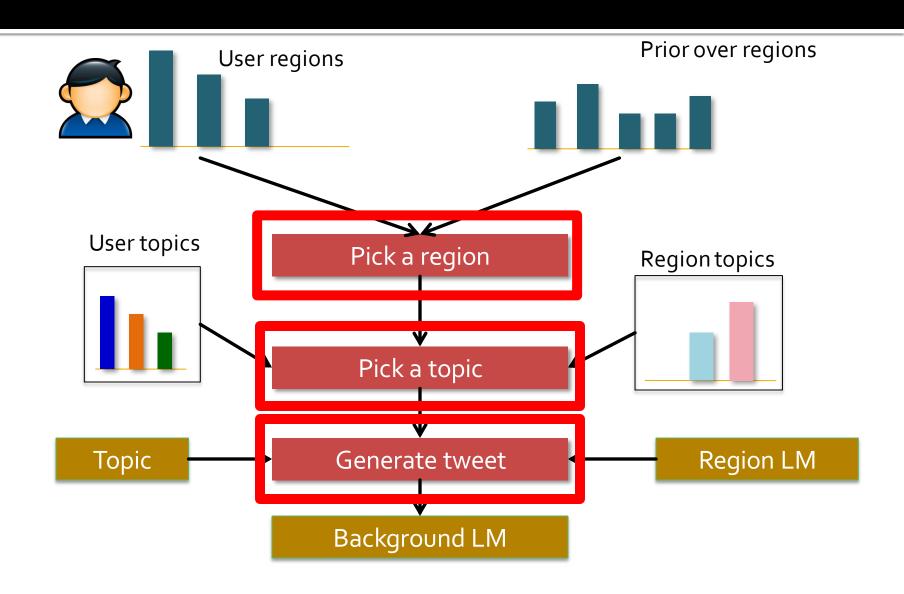
- Log-frequency differences
- Addition of multiple models Example:

$$P(v|\boldsymbol{\phi}_0, \boldsymbol{\phi}_u, \boldsymbol{\phi}_g) := p(v|\boldsymbol{\phi}_0 + \boldsymbol{\phi}_u + \boldsymbol{\phi}_g)$$

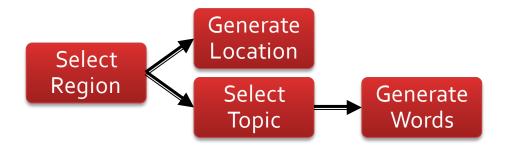
Use SAGE to replace "switch" variables to enable us incorporate multiple sources in different levels of our model easily

- Language models
 Example: background, regional, global...
- User preferences
 Example: global, regional, personal...

. . .



Generative Process



- Sparse Modeling
 - L_1 regularization (Laplace priors)
- Geographical Modeling
 - Bayesian treatment

Modeling Geographical Language Variations Inference Algorithm

- A variant of Monte Carlo EM
 - "E-Step": Sample latent discrete variables
 - "M-step": Update all model parameters
- Sparse update of gradients
- L_1 regularization: ISTA algorithm
- Initialize regions with K-means algorithm

Modeling Geographical Language Variations Experiments

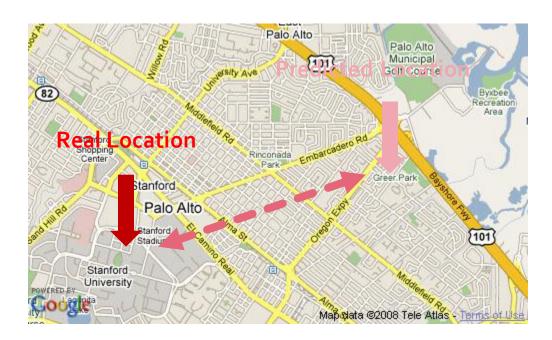
Dataset

- Twitter data
 - Randomly sample 1,000 users
 - All tweets from Jan 2011 to May 2011
 - 573,203 distinct tweets
- Twitter geographical data
 - Locations + Twitter Places

Modeling Geographical Language Variations Experiments

Location Prediction

- Metric
 - average error distance
 - Kilometers

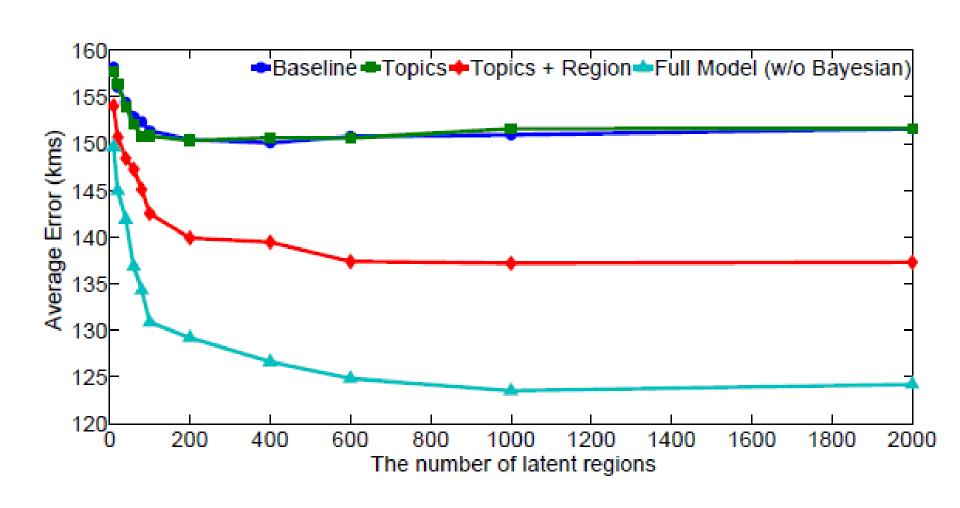


Modeling Geographical Language Variations Experiments

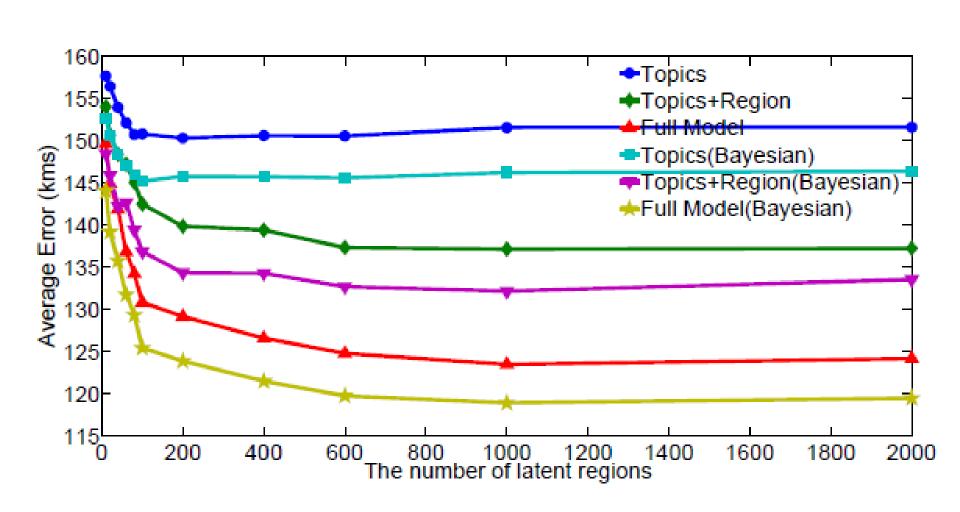
Location Prediction

- Baselines
 - [Yin et al. WWW 2011] paper
 - PLSA formalism
 - No personalization
 - Our model without $\phi^{\text{geo}} \eta^{\text{user}}$ and θ^{user}
 - Similar to Yin et al.'s formalism but SAGE model
 - Our model without η^{user} and θ^{user}

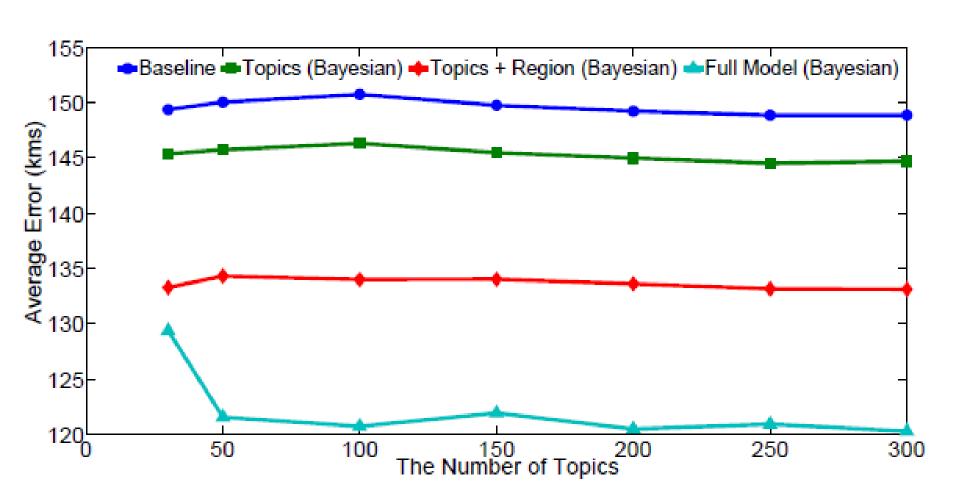
Modeling Geographical Language Variations Location Prediction



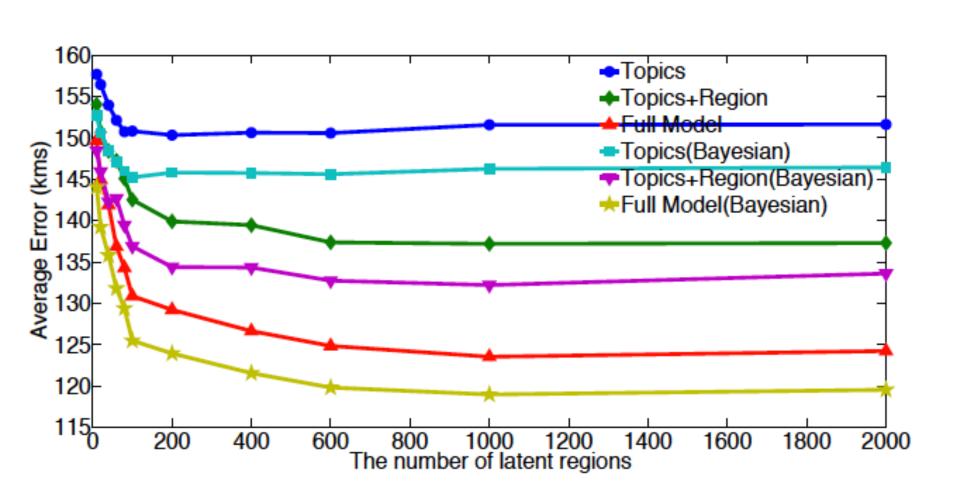
Modeling Geographical Language Variations Bayesian Treatment



Modeling Geographical Language Variations Number of Topics



Modeling Geographical Language Variations Number of Regions



Modeling Geographical Language Variations Experiments (Public Data)

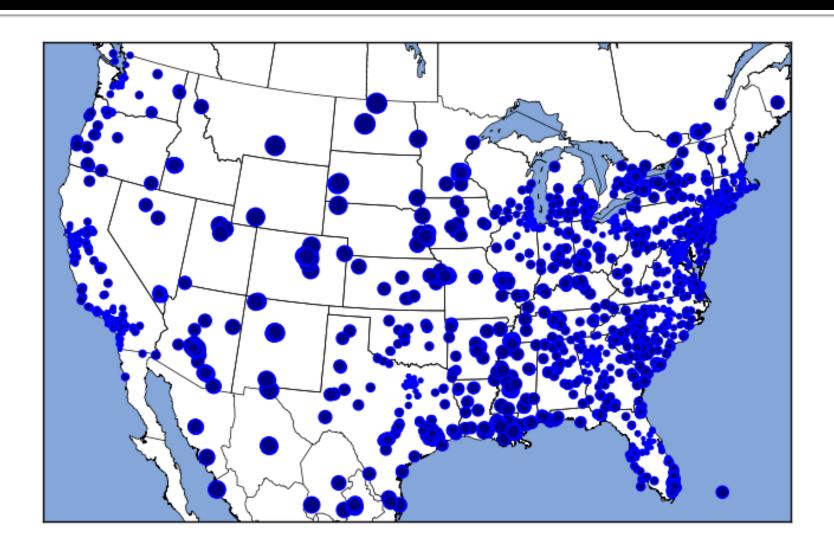
# of regions	[3]	[2]	[1]	Topics	Topics + Region	Full Model
10	494	479	501	540.60	481.58	449-45
20	494	479	501	522.18	446.03	420.83
40	494	479	501	513.06	414.95	395.13
60	494	479	501	507.37	410.09	380.04
80	494	479	501	499.42	408.38	374.01
100	494	479	501	498.94	407.78	372-99

^[1] Eisenstein et al. EMNLP 2010.

^[2] Wing and J. Baldridge. ACL 2011.

^[3] Eisenstein, Ahmed, Xing ICML 2011.

Modeling Geographical Language Variations Error Analysis



Modeling Geographical Language Variations Global and local topics

Entertainments

lady bieber album music beats artist video listen itunes apple produced movies #bieber lol new songs

Sports

yankees match nba football giants wow win winner game weekend horse #nba

Politics

obama election middle east china uprising egypt russian tunisia #egypt afghanistan people eu

Location with Top Ranked Terms

United States->New York->Brooklyn

brooklyn ave flatbush avenue mta prospect 5th #brooklyn spotlight carroll bushwick museum broadway madison vanderbilt coney slope eastern subway new york pkwy #viernesnayobon #mets otsego greenwich starbucks

United States->California->San Francisco

sfo francisco san airport international millbrae terminal flight burlingame bart mateo boarding bayshore telecommute landed heading bay airlines united bound flying #sfo camino groupon caltrain moon tsa baggage california engineer valley

United States->Pennsylvania->Philadelphia

philadelphia #philadelphia phl #jobs market others #job street philly walnut septa chestnut the cherry sansom arch spruce citizens locust btw temple pennsylvania rittenhouse passyunk bitlyetq7a6 bookrenters pike international

United Kingdom->England->London

winds lhr hounslow terminal the cloudy mph ickenham bath heathrow temperature airport car only airways uxbridge sun splendid fair london british lounge tothers harmondsworth speedbird when for stars day flight dominos navigation brunel

Australia->New South Wales->Sydney

sydney #sydney bondi george street mascot domestic syd surry station cnr platforms harbour darlinghurst qantas hoteloxford eddy haymarket terminal wales australia chalmers uts pitt #marketing junction darling centre #citijobs citigroup druitt

Modeling Geographical Language Variations Conclusions

- Probabilistic model for geographical information
 - Regional variations
 - Personal preferences
- Effective inference algorithm
- Best location prediction
- Discriminatively learned language models
- Future work
 - Hierarchical model
 - Hash tags
 - Temporal location model

A little bit more about me ...

- Ph.D. candidate at Lehigh (5.5 years)
- Published 10+ technical papers
 - KDD (3), SIGIR (2[1]), WWW (1[2]), WSDM (1), AAAI (1) and CIKM ([1])
 - Best Poster in WWW 2011
- Four internships
 - Yahoo! Labs (2010, 2011)
 - LinkedIn (2011)
 - A local software company (2008)
- Collaborated with Alex Smola (Google), Amr Ahmed (Google), Marco Pennacchiotti (eBay), Siva Gurumurthy (Twitter), Kostas Tsioutsiouliklis (Twitter), Jian Guo (Harvard Univ.), Ron Bekkerman (LinkedIn), Brian D. Davison (Lehigh Univ.), Dawei Yin (Lehigh Univ.), Ovidiu Dan (Microsoft), Zaihan Yang (Lehigh Univ.), Zhenzhen Xue (Google)

Questions?

Modeling Temporal Dynamics Handling Multiple Sources

Generative Process

- 1. For all common topics T_c , draw $\phi^{(c)} \sim \text{Dir}(\beta^{(c)})$
- 2. For a particular stream s
 - (a) For all local topics T_s , draw $\phi^{(s)} \sim \text{Dir}(\beta^{(s)})$
 - (b) For each document d in s
 - i. Draw Bernoulli parameter $\eta_{s,d} \sim \text{Beta}(\gamma_s^{(s)}, \gamma_s^{(c)})$
 - ii. Draw $\theta_d^{(s)} \sim \text{Dir}(\alpha_s)$
 - iii. Draw $\theta_d^{(c)} \sim \text{Dir}(\alpha_c)$

For each word position i in document d

- A. Draw $x_{di} \sim \text{Bernoulli}(\eta_{s,d})$
- B. Draw a topic $z_{di} \sim \text{Multinomial}(\theta_d^{(x_{di})})$
- C. Draw a word $w_{di} \sim \text{Multinomial } (\phi_{z_{di}}^{(x_{di})})$

Modeling Temporal Dynamics Handling Multiple Sources

Approximate Inference

Gibbs Sampling

$$p(x_{di} = s, z_{di} = t) \propto \frac{c_{d,s-i} + \gamma_s}{N_d + \gamma_s + \gamma_c - 1} \frac{m_{d,z-i} + \alpha_z}{\sum_{z \in T_s} m_{d,z-i} + \alpha_z} \frac{n_{z,w-i} + \beta_w^{(s)}}{\sum_w^V n_{z,w-i} + \beta_w^{(s)}}$$

$$p(x_{di} = c, z_{di} = t) \propto \frac{c_{d,c-i} + \gamma_c}{N_d + \gamma_s + \gamma_c - 1} \frac{m_{d,z-i} + \alpha_z}{\sum_{z \in T_c} m_{d,z-i} + \alpha_z} \frac{n_{z,w-i} + \beta_w^{(c)}}{\sum_w^V n_{z,w-i} + \beta_w^{(c)}}$$

Temporal Modeling

Temporal Function

$$V(t+1) = cf[V(t)]\delta(t)$$

- V(t): volume of the story
- f(v): a function of volume, encode "popularity"
- $\sigma(t)$: a function of time, encode "decay"

Temporal Modeling

Temporal Function

For some choices of function f and σ , we can analytically solve volume V(t):

$$A_k t^{M_k} \exp(-L_k t)$$

Temporal Modeling

Overall Algorithm

```
while not converge {f do}

E-step

For all documents in all text streams, update topic assignments using Equation (1)

M-step

Update {f lpha}, {f eta} and {f \gamma} values through the method introduced in [16] for each all local and common topics {f do}

1) Fit "Gaussian" function to {f lpha} values

2) Fit "Temporal Gamma" function by using the parameters from the previous step

3) Re-calculate {f lpha} values for topic {f k} by using fitted function end for end while
```

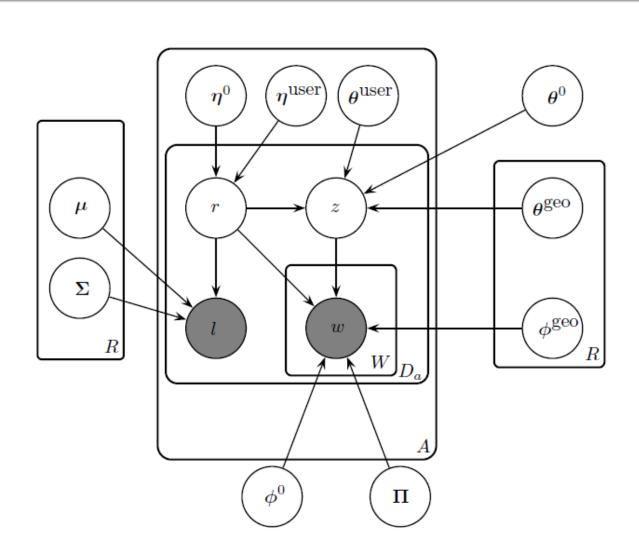
Hashtag	Top Terms of Mapped Topic	
[a] Hashtag Mapping for LDA model		
#mothersday	family home life children mother son friends	
#memorialday	event june call center community club park	
#bp	oil gulf spill coast mexico gas drilling	
#kentuckyderby	race car track kentucky win top cars	
#gaga & #justinbieber	justin lady super try bieber ider rio gaga jonas	
[b] Hashtag Mapping for Temporal Collection model		
#mothersday	family children day home life church mother	
#memorialday	memorial event day june community center	
#bp	oil gulf spill coast drilling mexico water louisiana	
#kentuckyderby	derby race borel kentucky horse super	
#gaga & #justinbieber	bieber music video song gaga album lady	

Modeling Geographical Language Variations Generative Process: Details

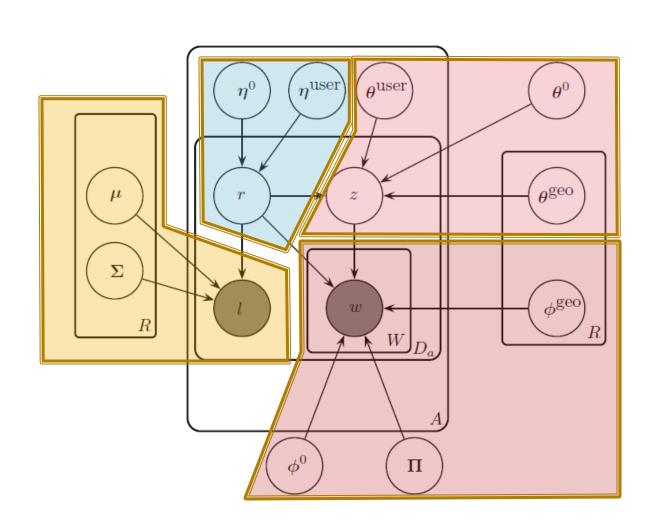
Notations

Symbol	\mathbf{Size}	Usage
$oldsymbol{\eta}^0$	$1 \times \mathbb{R}$	global region distribution
$oldsymbol{\eta}^{ ext{user}}$	$\mathbb{U} \times \mathbb{R}$	user-dependent region distribution
$oldsymbol{ heta}^0$	$1 \times \mathbb{K}$	global topic distribution
$m{ heta}^{ m geo}$	$\mathbb{R} imes \mathbb{K}$	region-dependent topic distribution
$oldsymbol{ heta}^{ ext{user}}$	$\mathbb{U} \times \mathbb{K}$	user-dependent topic distribution
$oldsymbol{\phi}^0$	$1 \times \mathbb{V}$	global term distribution
$oldsymbol{\phi}^{ ext{geo}}$	$\mathbb{R} imes \mathbb{V}$	region-dependent term distribution
Π	$\mathbb{K} imes \mathbb{V}$	a global topic matrix
$oldsymbol{\mu}$	\mathbb{R}^2	mean location of a latent region
Σ	$\mathbb{R}^{2 imes2}$	covariance matrix of a latent region

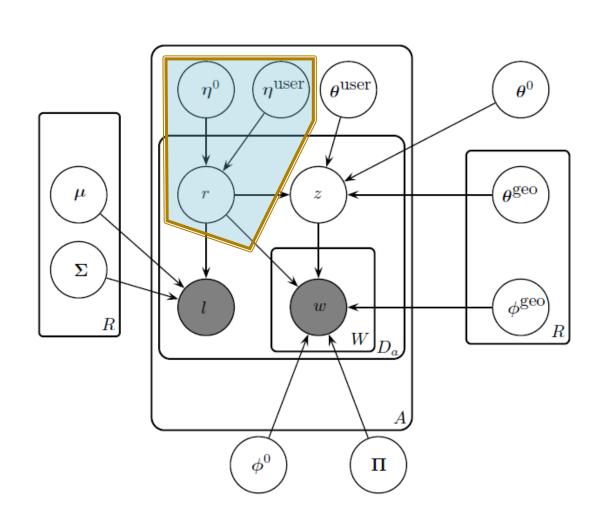
Modeling Geographical Language Variations The Graphical Model



Modeling Geographical Language Variations The Graphical Model



Modeling Geographical Language Variations Region Selection



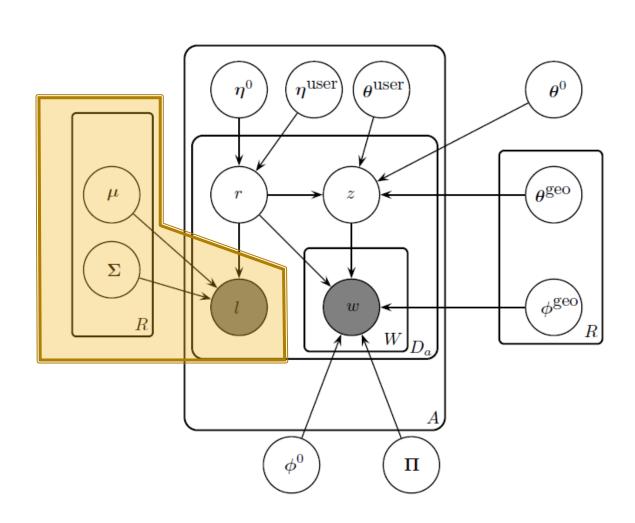
Modeling Geographical Language Variations Region Selection

Step-by-Step

Users tend to appear in a handful geographical locations.

$$P(r|\boldsymbol{\eta}^0, \boldsymbol{\eta}_u^{\text{user}}) = p(r|\boldsymbol{\eta}^0 + \boldsymbol{\eta}_u^{\text{user}})$$

Modeling Geographical Language Variations Location Generation

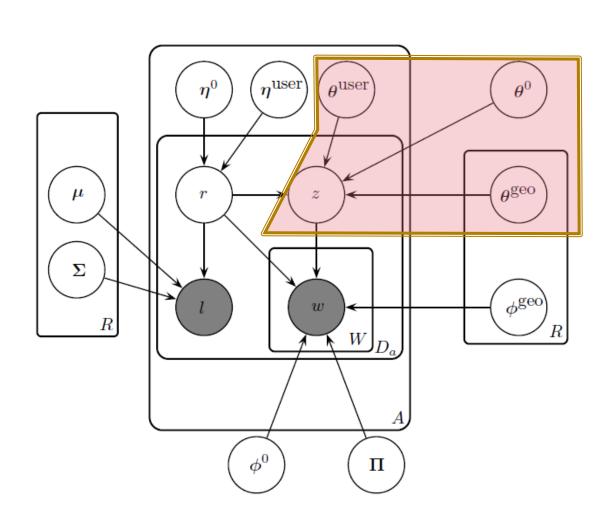


Modeling Geographical Language Variations Location Generation

Once a region is selected, locations can be generated.

$$\mathbf{l}_d \sim \mathcal{N}(\boldsymbol{\mu}_r, \boldsymbol{\Sigma}_r).$$

Modeling Geographical Language Variations Topic Selection

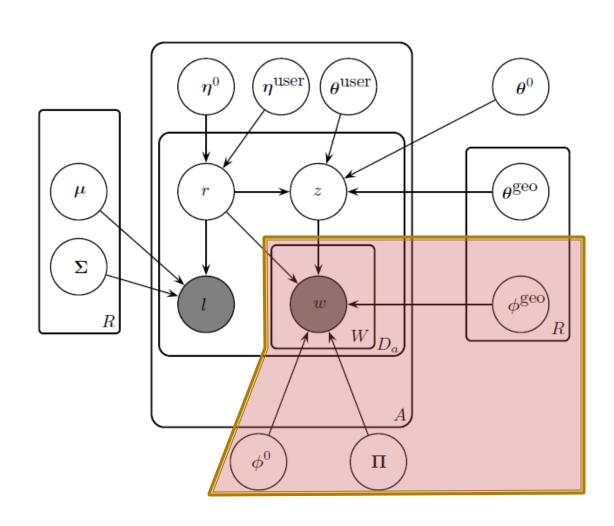


Modeling Geographical Language Variations Topic Selection

 Topics have different chances to be discussed in different regions by different users

$$P(z|\theta^0, \theta_u^{\text{user}}, \theta_r^{\text{geo}}) = p(z|\theta_j^0 + \theta_{u,j}^{\text{user}} + \theta_{r,j}^{\text{geo}})$$

Modeling Geographical Language Variations Word Generation



Modeling Geographical Language Variations Word Generation

 Words used in a tweet depend on both the location and topic of the tweet.

$$P(w|z, \phi^0, \phi_r^{\text{geo}}, \mathbf{\Pi}_z) = p(w|\phi^0 + \phi_r^{\text{geo}} + \mathbf{\Pi}_{z_d})$$

Modeling Geographical Language Variations Sparse Modeling

Laplace Priors

$$\eta_r^0 \sim \mathcal{L}(0, \omega^0) \quad \eta_{u,r}^{\text{user}} \sim \mathcal{L}(0, \omega_u)$$
 $\theta_z^{\text{geo}} \sim \mathcal{L}(0, \lambda_l) \quad \theta_{u,z}^{\text{user}} \sim \mathcal{L}(0, \lambda_u) \quad \theta_{r,z}^{\text{geo}} \sim \mathcal{L}(0, \lambda_r)$
 $\phi_v^0 \sim \mathcal{L}(0, \psi^0) \quad \phi_{r,v}^{\text{geo}} \sim \mathcal{L}(0, \psi_l)$
 $\Pi_{z,v} \sim \mathcal{L}(0, \psi_t)$

Sparsity results in predictive models

Modeling Geographical Language Variations Bayesian treatment

- Prior distributions over mean and covariance matrix
- Jeffery prior

$$\mu \sim \text{Unif.}$$

$$P(\mathbf{\Sigma}) \propto |\mathbf{\Sigma}|^{-(3/2)}$$
.

- Penalize large regions
 - We want region to be predictive as much as the data supports